Design of Underground Water Tank (Reservoir)

**Tank Dimensions**

Total area for the four floors = $4 \times (16 + 14 + 14) \times (13 + 14 + 13) = 7040 \text{ ft}^2$

:. Number of residents, $N = 7040 \times 8/1000 = 56$

:. Daily water requirement $= 56 \times 5 = 280 \text{ ft}^3$

:. Required volume of UG water tank, $V = 2 \times 280 = 560 \text{ ft}^3$

:. Depth of tank, $H = V^{1/3} = (560)^{1/3} = 8.24'$

Freeboard, F.B. = 0.50' $\Rightarrow$ Total depth, $D = H + \text{F.B.} = 8.74'$

Assuming $L/B = 1.5$, Tank area $A = LB$

:. $560/8.24 = 1.5B \Rightarrow B = 6.73'$, $L = 10.10'$

**Loads and Material Properties**

Loads: $FF = 10 \text{ psf}, LL = 20 \text{ psf}$

Materials: $f_c = 3 \text{ ksi}, f_{ult} = 5\sqrt{f_c} = 5\sqrt{3/1000} = 0.274 \text{ ksi}, f_{ult} = f_{ult}/2 = 0.137 \text{ ksi}, f_s = 20 \text{ ksi}$

:. $f_c = 0.45f_c = 1.35 \text{ ksi}, k = 0.378, j = 0.874, R = 0.223 \text{ ksi}, R_t = f_{ult}/6 = 0.023 \text{ ksi}$

For soil, Angle $\phi = 30^\circ \Rightarrow K_s = (1 - \sin \phi)/(1 + \sin \phi) = 0.333$

**Design Conditions**

The UG water tank has three basic components; i.e., top slab, sidewalls and base slab

- The top slab will be designed as normal simply supported slab based on the self-weight and superimposed loads
- The design of sidewalls and the base slab will be based on assuming
  (i) Tank full of water but no soil outside, (ii) No water inside tank but soil pressure from outside

The other more critical condition of no water inside but saturated soil outside is avoided here because it might cause instability of the tank itself. Alternately, a provision must be made that the tank cannot be evacuated when the soil is fully saturated.
Design of Top Slab

This is designed as a simply supported slab with clear spans

$S_a = 6.73'$, $S_b = 10.10'$, $m = 6.73/10.10 = 0.67$

Required slab thickness considering deflection = $2 \times (6.73 + 10.10)/15 = 2.24''$

Assuming minimum slab thickness $t = 4''$, $w_{\text{Total}} = 4 \times 150/12 + 10 + 20 = 80$ psf = 0.08 ksf

\[ C_a = 0.072 \Rightarrow M_a^{(+)} = 0.072 \times 0.08 \times (6.73)^2 = 0.261 \text{k}\ell'' \]

and $C_b = 0.014 \Rightarrow M_b^{(+)} = 0.014 \times 0.08 \times (10.10)^2 = 0.114 \text{k}\ell''$

\[ d_{\text{req}} = \sqrt{(M_{\text{max}}/R_b)} = \sqrt{(0.261/0.223)} = 1.08'' < d = 3'' \text{ or } 2.5'' \text{, OK} \]

\[ A_{sa}^{(+)} = M_a^{(+)}/f_{jd} = 0.261 \times 12/(20 \times 0.874 \times 3) = 0.06 \text{ in}^2/\ell'' \]

\[ A_{sb}^{(+)} = M_b^{(+)}/f_{jd} = 0.114 \times 12/(20 \times 0.874 \times 2.5) = 0.03 \text{ in}^2/\ell'' \]

\[ A_{s(\text{Temp})} = 0.03 t = 0.03 \times 4 = 0.12 \text{ in}^2/\ell'' \]

$S_{\text{max}} = 2t = 8'' \Rightarrow$ Use #3 @ 8" c/c in both directions

\[ A_\text{(A)}: \# 3 @ 8" \text{ c/c, alt. ckd. + 1 #3 extra top} \]

\[ A_\text{(B)}: \text{Corner reinforcement # 3 @ 8" c/c in both directions} \]
Design of Sidewalls

Since both L/H and B/H are within 0.5 and 2.0, both the sidewalls have both slab and cantilever action.

Cantilever action is within the bottom H/4 or 1 m height (whichever is greater).

H/4 = 8.24/4 = 2.06’, while 1 m = 3.28’ > 2.06’

Slab Action:

Case (i) – Tank full of water but no soil outside

In this case, \( p_{\text{max}} = \gamma_w (H-h) = 0.0625 \times (8.24-3.28) = 0.310 \text{ ksf} \)

Case (ii) – No water inside tank but soil pressure from outside

In this case, \( p_{\text{max}} = K_a \gamma_s (D-h) = 0.333 \times 0.120 \times (8.74-3.28) = 0.219 \text{ ksf} \)

The following bending moments \((k’/l’)) are obtained by analyzing the structure in GRASP

\[
\begin{align*}
\text{Case (i)} & \quad \text{Case (ii)} \\
\text{Cantilever Action:} & \quad \text{Cantilever Action:} \\
\text{Case (i) – Tank full of water but no soil outside} & \quad \text{Case (ii) – No water inside tank but soil pressure from outside} \\
\text{In this case, } p_{\text{max}} = \gamma_w H & \quad \text{In this case, } p_{\text{max}} = K_a \gamma_s D \\
& \quad 0.0625 \times 8.24 = 0.515 \text{ ksf} \\
\therefore \text{The maximum bending moment } M_{\text{max}} & \quad \therefore \text{The maximum bending moment } M_{\text{max}} \\
& \quad = p_{\text{max}} h^2/6 = 0.515 \times 3.28^2/6 = 0.924 k’/l’ \\
& \quad \text{Case (ii) – No water inside tank but soil pressure from outside} \\
\text{In this case, } p_{\text{max}} = K_a \gamma_s D & \quad 0.333 \times 0.120 \times 8.74 = 0.350 \text{ ksf} \\
\therefore \text{The maximum bending moment } M_{\text{max}} & \quad \therefore \text{The maximum bending moment } M_{\text{max}} \\
& \quad = p_{\text{max}} h^2/6 = 0.350 \times 3.28^2/6 = 0.627 k’/l’ \\
\therefore t_{\text{req}} = \sqrt{(M_{\text{max}}/R_b)} & \quad \therefore t_{\text{req}} = \sqrt{(2.049/0.023)} = 9.47” \Rightarrow t = 9.5” \quad \text{i.e., } d = 8”
\end{align*}
\]
\[ A_s = M/f_{jd} = M \times 12/(20 \times 0.874 \times 8) = M/11.65 \text{ in}^2/\]  
\[ A_{s(Temp)} = 0.03 t = 0.03 \times 9.5 = 0.29 \text{ in}^2/\]  
\[ S_{(\text{max})} = 2t = 19'' \]  
\[ \therefore \text{Since } M_{(\text{max})} = 2.049 k'/' \Rightarrow A_{s(\text{max})} = \frac{2.049}{11.65} = 0.18 \text{ in}^2/'' \]  
\[ \therefore A_{s(Temp)} \text{ governs in all cases; i.e., Use } #3 @ 4.5'' \text{ c/c on all surfaces in all directions} \]  

9.5'' thick Sidewalls

(A): # 3 @ 4.5'' c/c, on both faces and in both directions of the slab
(B): # 3 @ 4.5'' c/c, on both faces and in both directions of the slab
Design of Base Slab
Like the top slab, the base slab is also designed as a simply supported slab with clear spans
However, the slab has to carry end moments (0.924 k/" and 0.627 k/"") from the cantilever action of the sidewalls; which results in reduction of the midspan maximum moments.

\[ S_a = 6.73", \quad S_b = 10.10", \quad m = 6.73/10.10 = 0.67, \quad t_{\text{req}} = 2 (6.73 + 10.10)/15 = 2.24" \]

However since the slab carries significant load from water, the assumed slab thickness \( t = 7" \)

**Case (i) – Tank full of water but no soil outside**

\[ w_{\text{Total}} = \gamma t + \gamma_w H = 150 \times 7/12 + 10 + 62.5 \times 8.24 = 612.66 \text{ psf} = 0.613 \text{ ksf} \]

:. Assuming negative moment of 0.924 k/" \Rightarrow

\[ C_a = 0.072 \Rightarrow M_a^{(+)} = 0.072 \times 0.613 \times (6.73)^2 - 0.924 = 1.074 \text{ k/"} \]

and \( C_b = 0.014 \Rightarrow M_b^{(+)} = 0.014 \times 0.613 \times (10.10)^2 - 0.924 = -0.050 \text{ k/"} \)

**Case (ii) – No water inside tank but soil pressure from outside**

In this case, the total weight of top slab and sidewalls

\[ = \{(10.10 + 19/12) \times (6.73 + 19/12) \times 4/12 + 2 (10.10 + 6.73 + 19/12) \times 8.74 \times 9.5/12\} \times 0.15 = 43.08 \text{ k} \]

:. Net upward pressure from soil, \( w_{\text{Total}} = 43.08/\{(10.10 + 19/12) \times (6.73 + 19/12)\} = 0.444 \text{ ksf} \)

:. Assuming negative moment of 0.627 k/" \Rightarrow

\[ M_a^{(+)} = 0.072 \times 0.444 \times (6.73)^2 - 0.627 = 0.820 \text{ k/"} \]

\[ M_b^{(+)} = 0.014 \times 0.444 \times (10.10)^2 - 0.627 = 0.006 \text{ k/"} \]

:. \( t_{\text{req}} = \sqrt{(M_{\text{max}}/R_b)} = \sqrt{(1.074/0.023)} = 6.86" < t = 7" \), OK

:. \( t = 7" \Rightarrow d = 5.5" \): \( A_s = M/f_{jd} = M \times 12/(20 \times 0.874 \times 5.5) = M/8.01 \text{ in}^2/" \)

\[ A_{s(\text{Temp})} = 0.03 \times t = 0.03 \times 7 = 0.21 \text{ in}^2/" , \quad S_{(\text{max})} = 2t = 14" \]

:. Since \( M_{(\text{max})} = 1.074 \text{ k/"} \Rightarrow A_{s(\text{max})} = 1.074/8.01 = 0.13 \text{ in}^2/" \)

\[ A_{s(\text{Temp})} \text{ governs in all cases; i.e., since the sidewalls require #3 rods @ 4.5" c/c} \]

Use #3 @ 4.5" c/c on all surfaces in all directions
(A): # 3 @ 4.5" c/c, alt. ckd. + 1 #3 extra top
(B): Corner reinforcement # 3 @ 4.5" c/c in both directions

7” thick Base Slab