# University of Asia Pacific Department of Civil Engineering Final Examination, Spring- 2023 

Course Title: Principles of Management. Course Code : IMG 301. Credit : 2 Time : 02 Hours.<br>Marks: 50 .

Answer any 04 (Four) questions. All questions carry equal marks.

1. a) Distinguish Management and Leadership. ..... 4
b) Critically explain Charismatic Leadership Theory. ..... 8.5
2. a) What is Matrix Organization ? ..... 4
b) Delineate the advantages of Matrix Organization. ..... 8.5
3. a) Mention the key Characteristics of Teams. ..... 4
b) Critically examine the conflict management techniques. ..... 8.5
4. a) What is SWOT ? Give an example. ..... 4
b) Graphically represent Porter's Model ..... 8.5
5. Write short notes on: ..... 12.5
a) Power
b) Delegation of Authority

# University of Asia Pacific Department of Civil Engineering <br> Final Examination Spring 2023 <br> Program: B.Sc. in Civil Engineering 

## QUESTION 1 [20 MARKS]

a. An interior panel of flat slab of an office building (live load $2.4 \mathrm{kN} / \mathrm{m}^{2}$ ) is shown in Figure 1. The floor carries $2 \mathrm{kN} / \mathrm{m}^{2}$ dead load due to random wall and floor finishes. Minimum thickness of slab should be based on defection and punching requirements of code. The concrete strength ( $\mathrm{f}_{\mathrm{c}}$ ') could be used as $24 \mathrm{~N} / \mathrm{mm}^{2}$. Assume column size as $600 \mathrm{~mm} \times 600 \mathrm{~mm}$. Positive and negative moment coefficients of the panel are 0.35 and 0.65 respectively. Apply the concept to design the slab for long span only.


Figure 1. Panel of beam supported slab


Figure 2. Retaining wall
b. A cantilever retaining wall of an open underpass is shown in Figure 2. The density of soil beside the wall is $1700 \mathrm{~kg} / \mathrm{m}^{3}$, active soil pressure coefficient is 0.33 , soil is saturated with water (void ratio of the soil is $60 \%$ ). Apply the concept to design the wall with minimum thickness as per requirements of BNBC 2020. Assume required data for design, concrete strength (fc') could be used as $21 \mathrm{~N} / \mathrm{mm}^{2}$.

## QUESTION 2 [20 MARKS]

a. An interior column of a multi-storeyed academic building is subjected to dead and live loads of 2000 kN and 600 kN , respectively. The column is supported by an isolated pad footing, and the bearing capacity of soil under the footing is $200 \mathrm{kN} / \mathrm{m}^{2}$. Depth of the footing should be based on punching shear. Size of the column is $600 \mathrm{~mm} \times 600 \mathrm{~mm}$. Assume required concrete strength for optimal design (minimum thickness and steel) of square pad footing. Design the pad footing considering safety and environmental issues of design.
[14 Marks]
b. A 20 m span simply supported post-tensioned girder of an elevated express way is subjected to uniformly distributed $60 \mathrm{kN} / \mathrm{m}$ of dead load (including self-weight) and $30 \mathrm{kN} / \mathrm{m}$ live load. Eccentric tendon has to be used for economical design. The width of the girder could be assumed as 300 mm . The maximum allowable concrete compressive stress is $40 \mathrm{~N} / \mathrm{mm}^{2}$. Apply the concept
of pre-stressing to obtain required depth of girder for full prestressing. Assume eccentricity of tendon as 250 mm .
[6 Marks]

## QUESTION 3[20 MARKS]

The floor slab layout plan of a 9-storeyed Nurse Institute (Live load $2.4 \mathrm{kN} / \mathrm{m}^{2}$ ) is shown in Figure 3. The structure is constructed with frame structure, the slabs are supported by beams. The floor carries $3 \mathrm{kN} / \mathrm{m}^{2}$ dead load due to random wall and floor finishes. Design the short span of slab S1 (Figure 3). The moment of interior support is based on the consideration of continuous slab. Synthesis (optimize thickness and reinforcement) the design in accordance to deflection and shear requirements of ACI / BNBC code considering safety and environmental issues. Concrete compressive strength of the slab is $24 \mathrm{~N} / \mathrm{mm}^{2}$. Shear force co-efficient is 0.5 .
[20 Marks]


Figure 3: Floor Layout Plan of 9-Storeyed Nurse Institute

## QUESTION 4 [20 MARKS]

Design the column C1 (ground floor, Figure 3) of the structure stated in Question 3. The uni-axial design moment of the column at ground floor could be considered as $550 \mathrm{kN}-\mathrm{m}$, use approximate method to obtain design load of the column. Size of the column should be as minimal as possible applying all possible options of code (shape, concrete strength and steel ratio) with the consideration of safety and environmental issues of design. Propose a solution to design the column (tie column) with structural details.
[20 Marks]

## QUESTION 5 [20 MARKS]

The column "C1" as shown in Figure 3 of the structure stated in Question 3 is supported by pile foundation. The capacity of 600 mm diameter bore pile could be considered with the maximum value of 1000 kN . High strength concrete could be used to minimize the depth of pile cap. All possible options of code (BNBC) should be applied to minimize the depth and steel ratio in design. Provide a solution for economical (minimum depth, minimum steel) design of pile cap considering safety and environmental issues of design. Design equations of flexural and punching shear have to be formulated for high strength concrete to design the pile cap.
[20 Marks]

## University of Asia Pacific

Department of Civil Engineering
Final Examination Spring 2023
Program: B.Sc. Engineering (Civil)

Course Title: Environmental Engineering II
Time: 3.00 Hours

## There are five (5) questions. Answer all the questions. Assume any missing data. All questions bear equal marks [5 $\times 24=120]$

1. (a) Identify the problem of the presence of a tubewell closer to a common pitlatrine and your potential approaches to solve the adverse impacts. How could you solve the odor problems of such a common pit latrine?
(b) Calculate the maximum hourly, average daily, and minimum hourly residential sewage flows from an area occupied by 2000 people. The average per capita sewage flow is 50 gped. Consider the sewer length and house connections to be 2 miles and infiltration to be $40,000 \mathrm{gpd}$.
2. (a) Describe the factors that induce microbial sloughing in attached growth-based wastewater treatment reactors.
(b) Explain the operational mechanisms of an aeration tank and secondary clarifier of a typical activated sludge process.
3. Wastewater flow from an area averages $5000 \mathrm{~m}^{3} / \mathrm{d}$ during November (winter) and $8000 \mathrm{~m}^{3} / \mathrm{d}$ during June (summer). The average temperature in November is $8^{\circ} \mathrm{C}$, and the average in June (summer) is $32^{\circ} \mathrm{C}$. The mean concentration of influent $\mathrm{BOD}_{5}$ is $400 \mathrm{mg} / \mathrm{L}$. Reaction coefficient K is $0.23 \mathrm{~d}^{-1}$ at $20^{\circ} \mathrm{C}$, and $\theta$ is 1.06. Select a facultative pond treatment system for the area to remove $90 \%$ of the incoming BOD. Use the following graphical plot of the Thirumurthi equation if required.


Figure. Graphical plot of the Thirumurthi equation
4. (a) Identify the factors that allow the Bardenpho system to achieve better nitrogen removal from wastewater than the Pre D and Post D systems.
(b) Explain the role of external aeration in improving pollutant removal in vertical and horizontal flow wetlands with schematic diagrams.
5. You have been appointed to propose technology to treat tannery industry effluent. The concentration of the common parameters in the tannery effluent is given in the following table.

Table. Concentration of the common parameters

|  | Unit | Concentration |
| :--- | :--- | :--- |
| pH | --- | 11.5 |
| DO |  | 0.1 |
| $\mathrm{NH}_{4}-\mathrm{N}$ |  | 110 |
| $\mathrm{NO}_{3}-\mathrm{N}$ |  | 80 |
| TN |  | 240 |
| $\mathrm{BOD}_{5}$ | $\mathrm{mg} / \mathrm{L}$ | 2500 |
| COD |  | 10000 |
| TSS |  | 12000 |

Answer the following questions:
(i) Calculate the $\mathrm{BOD}_{5} / \mathrm{COD}$ ratio of the tannery effluent from the following table and report on the biodegradability of the wastewater.
(ii) Propose a natural-based treatment technology for treating such tannery effluent. Please note that there is limited land availability to construct wastewater treatment systems.
(iii) After 10 years of operation, a phosphorus concentration of $15 \mathrm{mg} / \mathrm{L}$ was detected in the same tannery effluent due to the use of phosphorus-based chemicals to process raw hides. Modify the existing treatment system for the removal of phosphorus. You cannot propose a new system as the limited land availability was completely utilized by the technology that was implemented according to your design 10 years ago.

# University of Asia Pacific <br> Department of Civil Engineering <br> Final Examination Spring 2023 <br> Program: B.Sc. Engineering (Civil) 

Course Title: Transportation Engineering I Time: 3 hours

Credit Hour: 3.00
Course Code: CE 351
Full Marks: 100

## Answer all the questions

1. a) Draw the configuration of an arterial road and identify its essential components.
b) Write down the name of grade separated interchange for three-legged interchange and draw the diagram with indicating the directions of traffic flow.
c) Discuss in brief the provisions of designing the following

$$
\begin{aligned}
\text { i. } & \text { Cul de sac } \\
\text { ii. } & \text { Staggered Intersection } \\
\text { iii. } & \text { Roundabout }
\end{aligned}
$$

2. a) Explain the disadvantages of traffic signal. Discuss the two methods of designing linked/ coordinated traffic signal.
b) Define all red period of a signal phase and describe where you should apply all red signal.
3. a) Between traffic signs and traffic markings, which one will you recommend to use in roads? Demonstrate why.
b) Write down the names of two types of special mandatory sign and explain where the traffic signs should be implied.
c) Explain peak hourly volume and design hourly volume.
4. Cherry intersection is to be converted into a two-phase signalized intersection for which the data are obtained as follows-

|  | North-South |  | East-West |
| :--- | :---: | :---: | :---: |
| Inter green period (s) | 9 | 10 |  |
| Starting lost time | (s) | 2 | 1 |
| End lost time | (s) | 1 | 1 |

If saturation rate (y) is $40 \%$ in both north and east(individually), while $20 \%$ in both south and west(individually) then
i) Design the signal
ii) Draw the concerned bar diagram
iii) Draw the phase diagram
$[10+6+4]$
5. The ratio of the cycle length and the effective green time at a signalized intersection is 2.5 .

The number of vehicles passing the intersection during the intervals of the saturation flow count is given as follows.

| Interval | Duration | PCU |
| :---: | :---: | :---: |
| First | 6 sec | 4 |
| Second | 6 sec | 12 |
| Third | 6 sec | 10 |
| Fourth | 6 sec | 10 |
| Fifth | 6 sec | 11 |
| Last | 3 sec | 2 |

i) Draw the saturation flow diagram and determine Saturation flow level.
ii) Calculate initial and final loss times.
iii) Determine approach capacity of the intersection.
6. A newly appointed traffic engineer studied a rural primary road. The annual average daily traffic (AADT) for the road is reported as 90,500 . To get an estimation on traffic variation over time, he back calculated traffic volume for 8 AM to $9 \mathrm{AM}, 11 \mathrm{AM}$ to 12 PM and 6 PM to 7 PM . The study was done on Friday, December 01. [See Annexure for necessary data]
i) Determine AWT for the mentioned month.
ii) Determine ADT for Wednesday.
iii) Determine when he will get the maximum traffic volume for the specified three time periods.
[5+4+6]

# University of Asia Pacific <br> Department of Civil Engineering <br> Final Examination Spring 2023 <br> Program: B.Sc. Engineering (Civil) 

Course Title: Engineering Hydrology
Time: 3 hours
Credit Hour: 3.0
Course Code: CE 363
Full Marks: 100

Answer all the questions $(10+20+25+20+25)$. The numbers inside the brackets indicate marks.
1 (a) Which factors should be considered in determining rainfall intensity using (5) rational formula?
(b) Define aquifer, aquitard and aquiclude.

2 (a) Discuss the hydrologic models and application of probability in hydrology.
(b) Discuss the suitability of lagging and S-curve method in determining unit (10) hydrograph.

3 (a) A schematic diagram of the stormwater drainage system is shown below. Using the rational method, determine the peak flow rates to be used in the sizing of pipes and inlets. Assume the flow velocity through the pipes is $2.5 \mathrm{ft} / \mathrm{s}$. The flow direction is given by the arrows.
Assume, Rainfall intensity, $\mathrm{i}=\frac{100}{(t+15)^{0.3}}$


| Basin | Area <br> $($ Acres $)$ | $\mathrm{t}_{\mathrm{i}}$ <br> $(\mathrm{min})$ | Runoff <br> Coefficient, C |
| :---: | :---: | :---: | :---: |
| A | 2.2 | 11 | 0.3 |
| B | 2.2 | 12 | 0.4 |
| C | 1.1 | 13 | 0.3 |
| D | 1.1 | 10 | 0.5 |
| E | 2.2 | 14 | 0.4 |
| F | 2.2 | 12 | 0.3 |
| G | 2.2 | 11 | 0.5 |


| Stormwater <br> Pipe | Length <br> $(\mathrm{ft})$ |
| :---: | :---: |
| $1-3$ | 200 |
| $2-3$ | 600 |
| $3-5$ | 200 |
| $4-5$ | 300 |

(b) A well penetrates an unconfined aquifer. Prior to pumping the water level, head is 30 m . After a long period of pumping at a constant rate of $0.04 \mathrm{~m}^{3} / \mathrm{s}$, the drawdown at a distance of 30 m and 75 m from the well were observed to be 3.2 m and 1 m , respectively. Estimate the hydraulic conductivity of the aquifer and radius of influence of the pumping well.

4 Find the first five values of outflow using level pool methodology. Area of the (20) reservoir is 1 acre.

| Time <br> $(\mathrm{min})$ | Inflow <br> $\left(\mathrm{ft}^{3} / \mathrm{s}\right)$ |
| :---: | :---: |
| 0 | 0 |
| 10 | 50 |
| 20 | 100 |
| 30 | 180 |
| 40 | 220 |
| 50 | 300 |
| 60 | 340 |
| 70 | 370 |
| 80 | 360 |
| 90 | 340 |
| 100 | 300 |
| 110 | 220 |
| 120 | 160 |
| 130 | 100 |
| 140 | 70 |
| 150 | 40 |
| 160 | 20 |
| 170 | 0 |
| 180 | 0 |
| 190 | 0 |
| 200 | 0 |


| Elevation <br> $(\mathrm{ft})$ | Discharge <br> $\left(\mathrm{ft}^{3} / \mathrm{s}\right)$ |
| :---: | :---: |
| 0 | 0 |
| 0.5 | 5 |
| 1 | 9 |
| 1.5 | 18 |
| 2 | 35 |
| 2.5 | 50 |
| 3 | 65 |
| 3.5 | 75 |
| 4 | 95 |
| 4.5 | 120 |
| 5 | 140 |
| 5.5 | 165 |
| 6 | 185 |
| 6.5 | 205 |
| 7 | 215 |
| 7.5 | 230 |
| 8 | 245 |
| 8.5 | 255 |
| 9 | 265 |
| 9.5 | 270 |
| 10 | 275 |

5 The annual maximum flood measured at a local valley for 19 years are given below. (25)

| Year | Max. Flood <br> $\left(\mathrm{ft}^{3} / \mathrm{s}\right)$ | Year | Max. Flood <br> $\left(\mathrm{ft}^{3} / \mathrm{s}\right)$ |
| :---: | :---: | :---: | :---: |
| 2001 | 4200 | 2011 | 4100 |
| 2002 | 2000 | 2012 | 3800 |
| 2003 | 5000 | 2013 | 3200 |
| 2004 | 4400 | 2014 | 4000 |
| 2005 | 3800 | 2015 | 3300 |
| 2006 | 3000 | 2016 | 7200 |
| 2007 | 2500 | 2017 | 5200 |
| 2008 | 2200 | 2018 | 1000 |
| 2009 | 3200 | 2019 | 650 |
| 2010 | 2400 |  |  |

Plot the data using the Weibull plotting position formula. Based on the frequency curve and the mathematical equation estimate the 15 -year annual maximum and the exceedance probability and return period for an event of $4000 \mathrm{ft}^{3} / \mathrm{s}$ using (i) lognormal and (ii) normal distribution. The standard deviation of normally and lognormally distributed data are 1524.19 and 0.25 , respectively.

Based on the statistical analysis used in (i) and (ii) investigate whether the data follows lognormal or normal distribution. If the data does not follow any of these distributions, what will you suggest. Justify your suggestions. Use the frequency factor table given below.

Table Frequency Factor for Normal Distribution

| Exceedance <br> Probability | Return Period | $\kappa$ | Exceedance <br> Probability | Return Period | $\kappa$ |
| :---: | :--- | :--- | :---: | :---: | :---: |
| 0.0001 | 10,000 | 3.719 | 0.450 | 2.22 | 0.126 |
| 0.0005 | 2,000 | 3.291 | 0.500 | 2.00 | 0.000 |
| 0.001 | 1,000 | 3.090 | 0.550 | 1.82 | -0.126 |
| 0.002 | 500 | 2.88 | 0.600 | 1.67 | -0.253 |
| 0.003 | 333 | 2.76 | 0.650 | 1.54 | -0.385 |
| 0.004 | 250 | 2.65 | 0.700 | 1.43 | -0.524 |
| 0.005 | 200 | 2.576 | 0.750 | 1.33 | -0.674 |
| 0.010 | 100 | 2.326 | 0.800 | 1.25 | -0.842 |
| 0.025 | 40 | 1.960 | 0.850 | 1.18 | -1.036 |
| 0.050 | 20 | 1.645 | 0.900 | 1.11 | -1.282 |
| 0.100 | 10 | 1.282 | 0.950 | 1.053 | -1.645 |
| 0.150 | 6.67 | 1.036 | 0.975 | 1.026 | -1.960 |
| 0.200 | 5.00 | 0.842 | 0.990 | 1.010 | -2.326 |
| 0.250 | 4.00 | 0.674 | 0.995 | 1.005 | -2.576 |
| 0.300 | 3.33 | 0.524 | 0.999 | 1.001 | -3.090 |
| 0.350 | 2.86 | 0.385 | 0.9995 | 1.0005 | -3.291 |
| 0.400 | 2.50 | 0.253 | 0.9999 | 1.0001 | -3.719 |

# University of Asia Pacific <br> Department of Civil Engineering <br> Final Examination Spring 2023 <br> Program: B.Sc. Engineering (Civil) 

Course Title: Structural Engineering II
Course Code: CE 313
Time: 3 hours
Credit Hour: 3.0
Full Marks: 100
ANSWER ALL QUESTIONS. Any missing data can be assumed reasonably.

## Part A

## QUESTION 1 [20 MARKS]

a. Analyze the frame shown in Figure 1 to calculate the horizontal deflection at $\mathbf{D}$ by the Unit Load Method [ $\mathrm{P}=35-\mathrm{kN}$ for Even Rolls or $\mathrm{P}=45-\mathrm{kN}$ for Odd Rolls and EI=Constant].
b. Analyze the truss shown in Figure 2 to obtain vertical deflection of joint 4 by the Unit Load Method [ $\mathrm{P}=20 \mathrm{kN}$ and $\mathrm{Q}=100 \mathrm{kN}$ for Even Rolls or $\mathrm{P}=28 \mathrm{kN}$ and $\mathrm{Q}=140 \mathrm{kN}$ for Odd Rolls and EA=Constant].
[10 Marks]


Figure 1


Figure 2

## QUESTION 2 [20 MARKS]

a. Analyze the beam in Figure 3 by Force Method and determine the reactions. Consider the vertical reaction at A or at C as the redundant [ $\mathrm{P}=40 \mathrm{kN}$ for Even Rolls or $\mathrm{P}=50 \mathrm{kN}$ for Odd Rolls and EI=Constant]
[10 Marks]
b. Analyze the frame in Figure 4 by Force Method and determine the support reactions. Consider the vertical reaction at D as redundant $[\mathrm{P}=20 \mathrm{kN}$ for Even Rolls or $\mathrm{P}=25 \mathrm{kN}$ for Odd Rolls and $\mathrm{EI}=$ Constant $]$.
[10 Marks]


Figure 3


Figure 4

## Part B

## QUESTION 3 [20 MARKS]

a. A frame of 10 -storeyed medical institute is subjected to lateral (wind) load as shown in Figure 5. Analyze the structure for lateral load using portal method to obtain shear force and bending moment of ground floor columns (C1, C2 and C3); shear force and bending moments of roof floor beams (B1, B2) using cantilever method. [Assume size of roof floor columns as C1: $500 \mathrm{~mm} \times 500 \mathrm{~mm} ; \mathrm{C} 2: 500 \mathrm{~mm} \times 750$ mm ; C3: $500 \mathrm{~mm} \times 1000 \mathrm{~mm}$ ]
[10 Marks]
b. Analyze the portal frame and truss of the industry building as shown in Figure 6 to obtain shear force and bending moment of columns ( C 1 and C 2 ); member forces of $\mathbf{a b}, \mathbf{a f}, \mathbf{b f}, \mathbf{b c}, \mathbf{b e}$ and $\mathbf{c f}$ of the truss. Assume that the diagonal members of truss could sustain compression force.
[10 Marks]


Figure 6: Truss of portal frame
Figure 5: Frame of Medical Institute

## QUESTION 4 [20 MARKS]

a. Draw the qualitative influence lines of the beam shown in Figure 7 for (I) Bending moments $\mathrm{M}_{\mathrm{C}}, \mathrm{M}_{\mathrm{G}}[\mathrm{G}$ is at mid-span of CD]; (II) Support reactions $R_{B}, R_{D}$ and (III) Shear forces $V_{B}{ }^{(L)}, V_{C}{ }^{(R)}$.
[6 Marks]

b. The supports and loading conditions of a continuous beam is shown in Figure 8. Analyze the structure using Moment Distribution Method to obtain moments (diagram) of beams. All beams have uniform cross- section.
[14 Marks]

## QUESTION 5 [20 MARKS]

The roof floor of RC frame of a building as shown in Figure 9 is subjected to design load of $45 \mathrm{kN} / \mathrm{m}$. The columns could be used as $600 \mathrm{~mm} \times 600 \mathrm{~mm}$ of normal strength concrete ( E is $29000 \mathrm{~N} / \mathrm{mm}^{2}$ ). Evaluate whether shear walls ( $300 \mathrm{~mm} \times 1200 \mathrm{~mm}$ ) of high strength concrete ( $E$ is $38000 \mathrm{~N} / \mathrm{mm}^{2}$ ) as replacements of three columns would increase or decrease the negative moments (at support) of beam ABC. Justify through comparative analysis of structure using moment distribution method. [Beam size as $300 \mathrm{~mm} \times 600 \mathrm{~mm}$ and E is $29000 \mathrm{~N} / \mathrm{mm}^{2}$ ].
$45 \mathrm{kN} / \mathrm{m}$
[20 Marks]



| $\int_{0}^{L} m m^{\prime} d x$ |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  | $m m^{\prime} L$ | $\frac{1}{2} m m^{\prime} L$ | $\frac{1}{2} m\left(m_{1}^{\prime}+m_{2}^{\prime}\right) L$ | $\frac{2}{3} m m^{\prime} L$ |
|  | $\frac{1}{2} m m^{\prime} L$ | $\therefore \frac{1}{3} m m^{\prime} L$ | $\cdots \frac{1}{6} m_{2}\left(m_{1}^{\prime}+2 m_{2}^{\prime}\right) L$ | $\frac{5}{12} m n^{\prime} L$ |
|  | $\frac{1}{2} m^{\prime}\left(m_{1}+m_{2}\right) L L$ | $\frac{1}{6} m^{\prime}\left(m_{1}+2 m_{2}\right) L$ | $\begin{aligned} & \frac{1}{6}\left[m_{1}^{\prime}\left(2 m_{1}+m_{2}\right)\right. \\ & \left.+m_{2}^{\prime}\left(m_{1}+2 m_{2}\right)\right] L \end{aligned}$ | $\frac{1}{12}\left[m^{\prime}\left(3 m_{1}+5 m_{2}\right)\right] L$ |
|  | $\frac{1}{2} m m^{\prime} L$ | $\frac{1}{6} m m^{\prime}(L+a)$ | $\begin{gathered} \frac{1}{5} m_{[ }\left[m_{1}^{\prime}(L+b)+\right. \\ \left.m_{2}(L+a)\right] \end{gathered}$ | $\frac{1}{12} m m^{\prime}\left(3+\frac{3 a}{L}-\frac{a^{2}}{L^{2}}\right) L$ |
| $m$ <br> $L$ | $\frac{1}{2} m n^{\prime} L$ | $\frac{1}{6} m m^{\prime} 2$ | $\frac{1}{6} m\left(2 m_{1}^{\prime}+m_{2}^{\prime}\right) L$ | $\frac{1}{4} m m^{\prime} \mathrm{L}$ |

Beam Deflections and Slopes

| Loading | $y+\uparrow$ | $\theta+5$ | Equation+ $\hat{\uparrow}+$ |
| :---: | :---: | :---: | :---: |
|  | $\begin{aligned} & v_{\max }=\frac{P L^{3}}{3 E I} \\ & \text { at } x=I \end{aligned}$ | $\begin{aligned} \theta_{\max } & =-\frac{P L^{2}}{2 E I} \\ \text { at } x & =L \end{aligned}$ | $v=\frac{P}{6 E I}\left(x^{3}-3 L x^{2}\right)$ |
|  | $\text { at } x=l$ | $\begin{aligned} & =\frac{B L}{L} \\ \text { at } x & =L \end{aligned}$ | $u=\frac{\Delta y_{0}}{24 i} x^{2}$ |

Fixed End Moments
$($ F

